



# basic education

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Department:  
Basic Education  
**REPUBLIC OF SOUTH AFRICA**

**SENIOR CERTIFICATE EXAMINATIONS/  
SENIORSERTIFIKAAT-EKSAMEN  
NATIONAL SENIOR CERTIFICATE EXAMINATIONS/  
NASIONALE SENIORSERTIFIKAAT-EKSAMEN**

**MATHEMATICS P2/WISKUNDE V2**

**MARKING GUIDELINES/NASIENRIGLYNE**

**MAY/JUNE/MEI/JUNIE 2023**

**MARKS: 150  
PUNTE: 150**

**These marking guidelines consist of 21 pages./  
Hierdie nasienriglyne bestaan uit 21 bladsye.**

**NOTE:**

- If a candidate answers a question TWICE, mark only the FIRST attempt.
- If a candidate has crossed out an attempt at an answer and not redone the question, mark the crossed-out version.
- Consistent accuracy applies in ALL aspects of the marking guidelines. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

**LET WEL:**

- As 'n kandidaat 'n vraag TWEE KEER beantwoord, sien slegs die EERSTE poging na.
- As 'n kandidaat 'n antwoord van 'n vraag doodtrek en nie oordoen nie, merk die doodgetrekte poging.
- Volgehoue akkuraatheid word in ALLE aspekte van die nasienriglyne toegepas. Hou op nasien by die tweede berekeningsfout.
- Aanvaar van antwoorde/waardes om 'n probleem op te los, word NIE toegelaat nie.

<b>GEOMETRY • MEETKUNDE</b>	
<b>S</b>	<b>A mark for a correct statement</b> <i>(A statement mark is independent of a reason)</i>
	<b>'n Punt vir 'n korrekte bewering</b> <i>('n Punt vir 'n bewering is onafhanklik van die rede)</i>
<b>R</b>	<b>A mark for the correct reason</b> <i>(A reason mark may only be awarded if the statement is correct)</i>
	<b>'n Punt vir 'n korrekte rede</b> <i>('n Punt word slegs vir die rede toegeken as die bewering korrek is)</i>
<b>S/R</b>	<b>Award a mark if statement AND reason are both correct</b>
	<b>Ken 'n punt toe as die bewering EN rede beide korrek is</b>

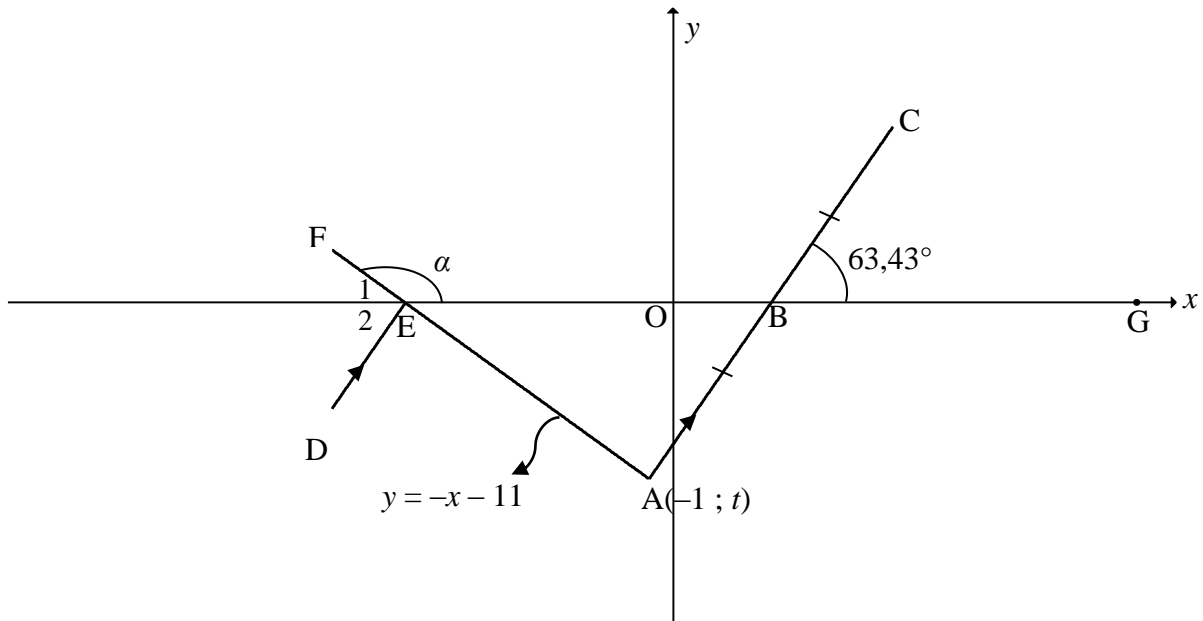
**QUESTION/VRAAG 1**

1.1.1	$a = 1730,22$ $b = 13,96$ $\hat{y} = 1730,22 + 13,96x$	$\checkmark a = 1730,22$ $\checkmark b = 13,96$ $\checkmark$ equation  (3)
1.1.2	$\hat{y} = 1730,22 + 13,96x$ $\hat{y} = 1730,22 + 13,96(28500)$ $\hat{y} = R399\ 590,22$  <b>OR/OF</b>  $\hat{y} = R399\ 599,64$ (calc)	$\checkmark$ substitution $\checkmark$ answer  (2)  $\checkmark\checkmark$ answer  (2)
1.1.3	$r = 0,98002 \dots$ $r = 0,98$	$\checkmark$ answer  (1)
1.1.4	<p>There is a very strong positive correlation between the amount spent on advertising and sales. /  <i>Daar is 'n baie sterk positiewe korrelasie tussen die bedrag spandeer op advertensie en die verkope.</i></p>	$\checkmark$ strong positive  (1)
1.2.1	$\bar{x} = \frac{1\ 552\ 195}{9}$ $\bar{x} = 172\ 466,11$	$\checkmark \bar{x} = \frac{1\ 552\ 195}{9}$ $\checkmark$ answer  (2)
1.2.2	$\sigma = 56950,09$	$\checkmark$ answer  (1)
1.2.3	$\bar{x} + \sigma$ $= 172\ 466,11 + 56950,09$ $= 229\ 416,20$  2 years/jaar	$\checkmark \bar{x} + \sigma$  $\checkmark$ answer  (2)
		<b>[12]</b>

**QUESTION/VRAAG 2**

2.1	$35 < x \leq 45$	✓ answer  (1)																								
2.2	320 people/mense	✓ answer  (1)																								
2.3	<table border="1" data-bbox="384 551 1067 913"> <thead> <tr> <th>AGE</th> <th>NUMBER OF PEOPLE</th> <th>CUMULATIVE FREQUENCY</th> </tr> </thead> <tbody> <tr> <td><math>5 &lt; x \leq 15</math></td> <td>20</td> <td>20</td> </tr> <tr> <td><math>15 &lt; x \leq 25</math></td> <td>25</td> <td>45</td> </tr> <tr> <td><math>25 &lt; x \leq 35</math></td> <td>60</td> <td>105</td> </tr> <tr> <td><math>35 &lt; x \leq 45</math></td> <td>90</td> <td>195</td> </tr> <tr> <td><math>45 &lt; x \leq 55</math></td> <td>55</td> <td>250</td> </tr> <tr> <td><math>55 &lt; x \leq 65</math></td> <td>40</td> <td>290</td> </tr> <tr> <td><math>65 &lt; x \leq 75</math></td> <td>30</td> <td>320</td> </tr> </tbody> </table> <div data-bbox="261 913 1166 1794" style="text-align: center;"> <p><b>OGIVE/OGIEF</b></p> </div>	AGE	NUMBER OF PEOPLE	CUMULATIVE FREQUENCY	$5 < x \leq 15$	20	20	$15 < x \leq 25$	25	45	$25 < x \leq 35$	60	105	$35 < x \leq 45$	90	195	$45 < x \leq 55$	55	250	$55 < x \leq 65$	40	290	$65 < x \leq 75$	30	320	<ul style="list-style-type: none"> <li>✓ cumulative frequency</li> <li>✓ grounding</li> <li>✓ plotting at upper limit</li> <li>✓ shape</li> </ul> <p style="text-align: right;">(4)</p>
AGE	NUMBER OF PEOPLE	CUMULATIVE FREQUENCY																								
$5 < x \leq 15$	20	20																								
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$55 < x \leq 65$	40	290																								
$65 < x \leq 75$	30	320																								
2.4	Median = 41	✓✓ answer  (2)																								
		<b>[8]</b>																								

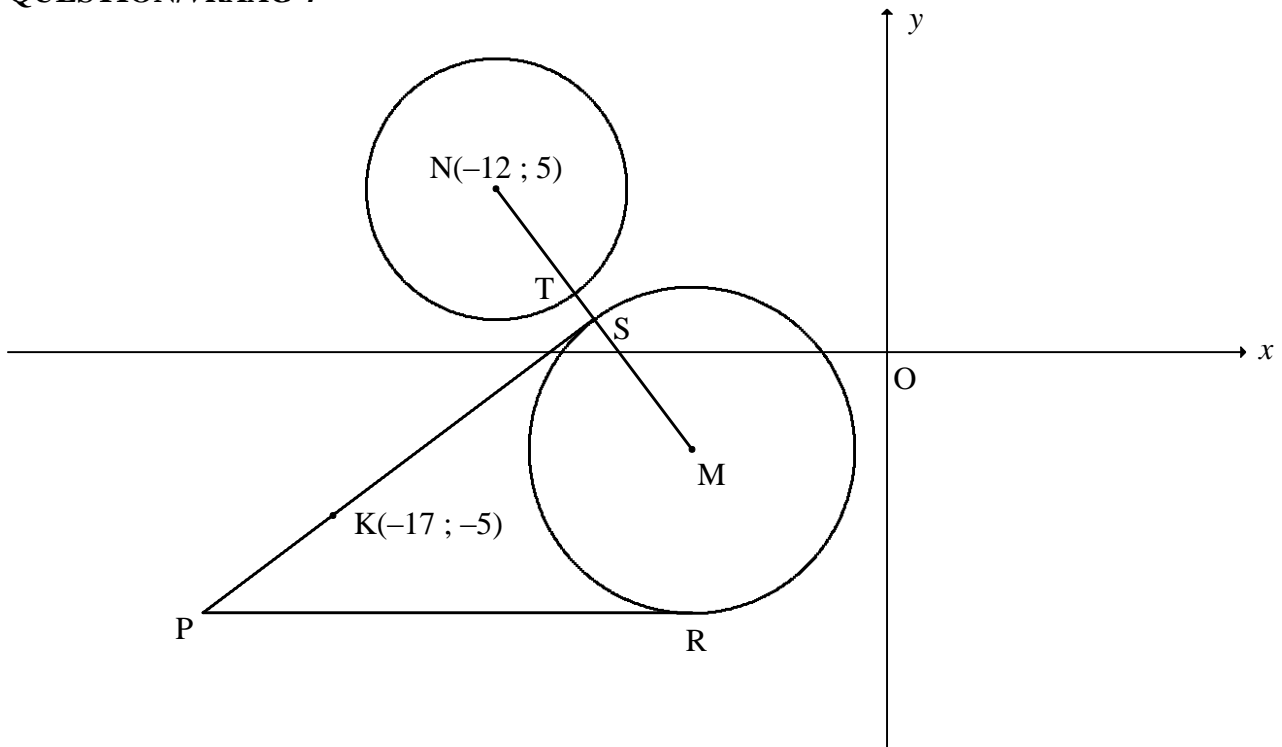
**QUESTION/VRAAG 3**



3.1.1	$y = -x - 11$ $A(-1 ; t)$ $t = -(-1) - 11$ $t = -10$	✓ substitution ✓ value of $t$ (2)
3.1.2	$\tan \alpha = -1$ $ref. \angle = 45^\circ$ $\therefore \alpha = 135^\circ$	✓ $\tan \alpha = -1$ ✓ $135^\circ$ (2)
3.1.3	$\tan 63,43^\circ = m_{AC}$ $m_{AC} = 2$	✓ $\tan 63,43^\circ = m_{AC}$ ✓ answer (2)
3.2	$m_{AC} = 2$ $A(-1 ; -10)$ $y = 2x + k$ $-10 = 2(-1) + k$ $k = -8$ $y = 2x - 8$	<p style="text-align: center;"><b>OR/OF</b></p> $y - y_1 = 2(x - x_1)$ $y - (-10) = 2(x - (-1))$ $y = 2x - 8$ ✓ substitution of $m$ and A ✓ equation (2)

<p>3.3.1</p>	<p><math>y = 2x - 8</math>  <math>0 = 2x - 8</math>  <math>x_B = 4</math></p> <p><math>\frac{x_C + (-1)}{2} = 4</math>                      <math>\frac{y_C + (-10)}{2} = 0</math>  <math>x_C = 9</math>                                      <math>y_C = 10</math></p> <p><b>OR/OF</b> by translation / <i>met translasie</i></p> <p><math>A \rightarrow B (x; y) \rightarrow (x + 5; y + 10)</math>  <math>B \rightarrow C (4; 0) \rightarrow (4 + 5; 0 + 10) = (9; 10)</math></p>	<p>✓ <math>x_B = 4</math></p> <p>✓ <math>x_C = 9</math>    ✓ <math>y_C = 10</math>  (3)</p> <p>✓ <math>(x + 5; y + 10)</math>  ✓ <math>x_C = 9</math>    ✓ <math>y_C = 10</math>  (3)</p>
<p>3.3.2</p>	<p><math>\hat{A}BE = 63,43^\circ</math>                      [vert. opp <math>\angle</math>'s =]  <math>\hat{E}_2 = 63,43^\circ</math>                      [corres. <math>\angle</math>'s, DE    AB]  <math>\hat{E}_1 = 45^\circ</math>                              [<math>\angle</math>s on a str line]  <math>\hat{F}ED = 108,43^\circ</math></p> <p><b>OR/OF</b></p> <p><math>\hat{E}AB = 135^\circ - 63,43^\circ</math>  <math>\hat{E}AB = 71,57^\circ</math>  <math>\hat{D}EA = \hat{E}AB = 71,57^\circ</math>  <math>\hat{F}ED = 108,43^\circ</math></p> <p><b>OR/OF</b></p> <p><math>\hat{A}BE = 63,43^\circ</math>                      [vert. opp <math>\angle</math>'s]  <math>\hat{D}EO = 116,57^\circ</math>                      [co-int. <math>\angle</math>'s, DE    AB]  <math>\hat{F}ED = 360^\circ - (116,57^\circ + 135^\circ)</math>  <math>= 108,43^\circ</math></p>	<p>✓ <math>\hat{A}BE = 63,43^\circ</math></p> <p>✓ <math>\hat{E}_1 = 45^\circ</math>  ✓ <math>\hat{F}ED = 108,43^\circ</math>  (3)</p> <p>✓ <math>\hat{E}AB = 71,57^\circ</math>  ✓ <math>\hat{D}EA = \hat{E}AB = 71,57^\circ</math>  ✓ <math>\hat{F}ED = 108,43^\circ</math>  (3)</p> <p>✓ <math>\hat{A}BE = 63,43^\circ</math>  ✓ <math>\hat{D}EO = 116,57^\circ</math>  ✓ <math>\hat{F}ED = 108,43^\circ</math>  (3)</p>
<p>3.4</p>	<p><math>y = 0</math>  <math>x_E = -11</math>  <math>\frac{x_G + (-11)}{2} = 4</math>  <math>x_G = 19</math></p> <p><math>(x - 19)^2 + y^2 = 15^2</math>  <math>(x - 19)^2 + y^2 = 225</math></p>	<p>✓ <math>x_E = -11</math></p> <p>✓ <math>x_G = 19</math></p> <p>✓ <math>(x - 19)^2 + y^2 = 225</math>  (4)</p>
<p><b>[18]</b></p>		

**QUESTION/VRAAG 4**



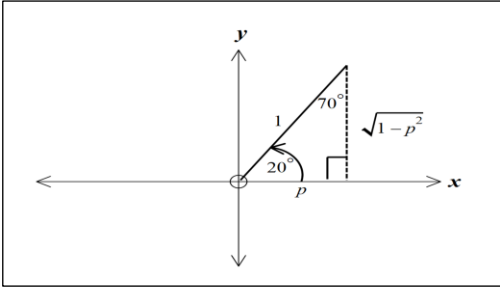
4.1	$M(-6; -3)$	✓ $-6$ ✓ $-3$ (2)
4.2.1	$x^2 + y^2 + 24x - 10y + 153 = 0$ $(x + 12)^2 + (y - 5)^2 = -153 + 144 + 25$ $(x + 12)^2 + (y - 5)^2 = 16$ $r^2 = 16$ $r = 4$ units	✓ $r^2 = -153 + 144 + 25$ ✓ length of radius (2)
4.2.2	$NM = \sqrt{(-12 - (-6))^2 + (5 - (-3))^2}$ $NM = 10$ units $SM = 5$ units $\therefore TS = 10 - 5 - 4 = 1$ unit	✓ substitution into distance formula ✓ $NM = 10$ units ✓ $SM = 5$ units ✓ answer (4)
4.3.1	$R(-6; -8)$ $y = -8$	✓ $y_R = -8$ ✓ answer (2)

<p>4.3.2</p>	$m_{NM} = \frac{5 - (-3)}{-12 - (-6)}$ $m_{NM} = -\frac{4}{3}$ $m_{\text{tangent}} = \frac{3}{4}$ $-5 = \frac{3}{4}(-17) + c \quad \text{OR/OF} \quad y - y_1 = \frac{3}{4}(x - x_1)$ $c = \frac{31}{4} \quad y - (-5) = \frac{3}{4}(x - (-17))$ $y = \frac{3}{4}x + \frac{31}{4} \quad y = \frac{3}{4}x + \frac{31}{4}$ <p><b>OR/OF</b></p> <p>NS = SM = 5</p> <p>S <math>\left(\frac{-12-6}{2}; \frac{5-3}{2}\right)</math></p> <p>S (-9 ; 1)</p> $m_{SK} = \frac{1 - (-5)}{-9 + 17}$ $= \frac{6}{8} = \frac{3}{4}$ $y + 5 = \frac{3}{4}(x + 17)$ $y = \frac{3}{4}x + \frac{31}{4} \text{ or } y = \frac{3}{4}x + 7\frac{3}{4}$	<p>✓ substitution</p> <p>✓ <math>m_{NM} = -\frac{4}{3}</math></p> <p>✓ <math>m_{\text{tangent}} = \frac{3}{4}</math></p> <p>✓ substitution of <math>m</math> and N</p> <p>✓ equation (5)</p> <p>✓ S midpoint</p> <p>✓ coordinates of S</p> <p>✓ <math>m_{\text{tangent}} = \frac{3}{4}</math></p> <p>✓ substitution of <math>m</math> and K(-17 ; -5) or S</p> <p>✓ equation (5)</p>
<p>4.4.1</p>	$-8 = \frac{3}{4}x + \frac{31}{4}$ $-32 = 3x + 31$ $3x = -63$ $x = -21$ <p>P(-21 ; -8)</p> <p>R(-6 ; -8)</p> <p>PR = PS = 15 units [tangents from same point]</p> <p>MS = MR = 5 units</p> <p>Perimeter PSMR = 15 + 15 + 5 + 5</p> <p style="text-align: center;">= 40 units</p>	<p>✓ <math>-8 = \frac{3}{4}x + \frac{31}{4}</math></p> <p>✓ <math>x = -21</math></p> <p>✓ PR = PS = 15 units</p> <p>✓ MS = MR = 5 units</p> <p>✓ answer (5)</p>



<p>4.4.2</p>	$\frac{\text{area of } \triangle NPS}{\text{area of quadrilateral PSMR}}$ $\frac{\frac{1}{2} NS.SP}{\frac{1}{2} SP.MS + \frac{1}{2} MR.PR}$ $= \frac{\frac{1}{2}(5)(15)}{2\left(\frac{1}{2}\right)(5)(15)}$ $= \frac{1}{2}$ <p><b>OR</b></p> $\triangle NPS \equiv \triangle SPM \equiv \triangle MPR$ $\frac{\text{area of } \triangle NPS}{\text{area of quadrilateral PSMR}}$ $= \frac{1}{2}$	<p>✓ substitution</p> <p>✓ answer (2)</p> <p>✓ congruent</p> <p>✓ answer (2)</p>
<p><b>[22]</b></p>		

**QUESTION/VRAAG 5**

<p>5.1</p>	$\frac{1 - \sin(-\theta)\cos(90^\circ + \theta)}{\cos(\theta - 360^\circ)}$ $= \frac{1 - (-\sin\theta)(-\sin\theta)}{\cos\theta}$ $= \frac{1 - \sin^2\theta}{\cos\theta}$ $= \frac{\cos^2\theta}{\cos\theta}$ $= \cos\theta$	<p>✓ <math>-\sin\theta</math> ✓ <math>-\sin\theta</math>                  ✓ <math>\cos\theta</math></p> <p>✓ <math>\cos^2\theta</math>                  ✓ answer</p> <p>(5)</p>
<p>5.2.1</p>	$\cos 200^\circ$ $= -\cos 20^\circ$ $= -p$	<p>✓ reduction                  ✓ answer</p> <p>(2)</p>
<p>5.2.2</p>	$\sin(-70^\circ)$ $= -\sin 70^\circ$ $= -\cos 20^\circ$ $= -p$ <p><b>OR/OF</b></p> $\sin(-70^\circ)$ $= -\sin 70^\circ$ $= -p$	<p>✓ reduction                  ✓ answer</p>  <p>✓ reduction                  ✓ answer</p> <p>(2)</p>
<p>5.2.3</p>	$\sin 10^\circ$ $\cos(2(10^\circ)) = 1 - 2\sin^2 10^\circ$ $2\sin^2 10^\circ = 1 - \cos 20^\circ$ $\sin 10^\circ = \sqrt{\frac{1 - \cos 20^\circ}{2}}$ $\sin 10^\circ = \sqrt{\frac{1 - p}{2}}$ <p><b>OR/OF</b></p> $\sin 10^\circ$ $\sin(30^\circ - 20^\circ)$ $= \sin 30^\circ \cos 20^\circ - \cos 30^\circ \sin 20^\circ$ $= \frac{1}{2}p - \frac{\sqrt{3}}{2}\sqrt{1-p^2} = \frac{p - \sqrt{3}\sqrt{1-p^2}}{2}$ <p><b>OR/OF</b></p>	<p>✓ double angle</p> <p>✓ <math>\sin 10^\circ</math> as subject</p> <p>✓ answer</p> <p>(3)</p> <p>✓ using special angle                  ✓ expanding</p> <p>✓ answer</p> <p>(3)</p>

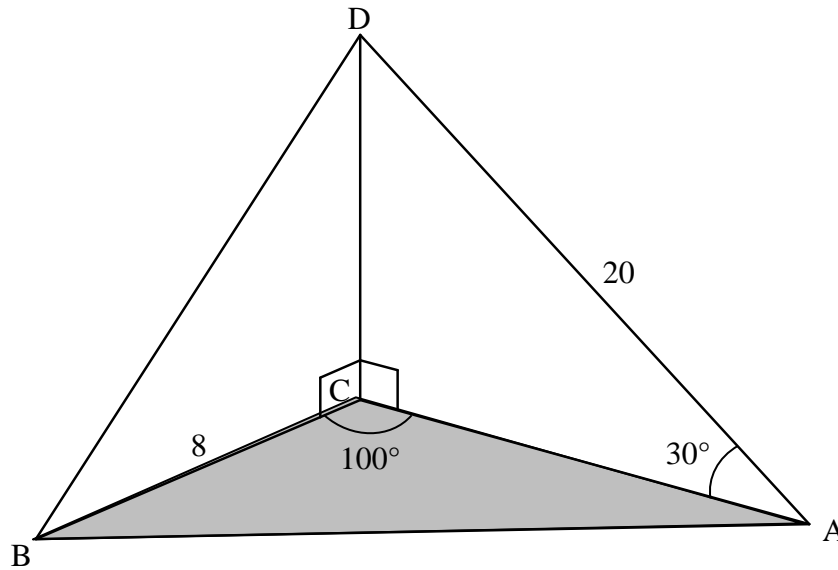
	$\sin 10^\circ$ $\sin(70^\circ - 60^\circ)$ $= \sin 70^\circ \cos 60^\circ - \cos 70^\circ \sin 60^\circ$ $= p \cdot \frac{1}{2} - \sqrt{1-p^2} \times \frac{\sqrt{3}}{2} = \frac{p - \sqrt{3}\sqrt{1-p^2}}{2}$ <p><b>OR/OF</b></p> $\sin 10^\circ$ $= \cos 80^\circ$ $\cos(60^\circ + 20^\circ)$ $= \cos 60^\circ \cos 20^\circ - \sin 60^\circ \sin 20^\circ$ $= \frac{1}{2} p - \frac{\sqrt{3}}{2} \cdot \sqrt{1-p^2}$	<p>✓ using special angle ✓ expanding</p> <p>✓ answer (3)</p> <p>✓ using special angle ✓ expanding</p> <p>✓ answer (3)</p>
<p>5.3</p>	$\cos(A + 55^\circ)\cos(A + 10^\circ) + \sin(A + 55^\circ)\sin(A + 10^\circ)$ $= \cos[A + 55^\circ - (A + 10^\circ)]$ $= \cos 45^\circ$ $= \frac{1}{\sqrt{2}} \quad \text{or} \quad \frac{\sqrt{2}}{2}$	<p>✓✓ compound identity</p> <p>✓ answer (3)</p>
<p>5.4.1</p>	$\text{LHS} = \frac{\cos 2x + \sin 2x - \cos^2 x}{\sin x - 2 \cos x}$ $= \frac{\cos^2 x - \sin^2 x + 2 \sin x \cos x - \cos^2 x}{\sin x - 2 \cos x}$ $= \frac{-\sin^2 x + 2 \sin x \cos x}{\sin x - 2 \cos x}$ $= \frac{-\sin x(\sin x - 2 \cos x)}{\sin x - 2 \cos x}$ $= -\sin x$ <p>∴ LHS = RHS</p> <p style="text-align: right;"><math>\text{RHS} = -\sin x</math></p>	<p>✓ <math>\cos^2 x - \sin^2 x</math> ✓ <math>2 \sin x \cos x</math></p> <p>✓ common factor of <math>-\sin x</math></p> <p>(3)</p>
<p>5.4.2</p>	$\frac{\cos 2x + \sin 2x - \cos^2 x}{-3 \sin^2 x + 6 \sin x \cos x}$ $= \frac{\cos 2x + \sin 2x - \cos^2 x}{-3 \sin x(\sin x - 2 \cos x)}$ $= \frac{\cos 2x + \sin 2x - \cos^2 x}{(\sin x - 2 \cos x)} \times \frac{1}{-3 \sin x}$ $= (-\sin x) \times \frac{1}{-3 \sin x}$ $= \frac{1}{3}$	<p>✓ common factor of <math>-3 \sin x</math></p> <p>✓ substitution</p> <p>✓ answer (3)</p>

5.5.1	$3 \tan 4x = -2 \cos 4x$ $3 \left( \frac{\sin 4x}{\cos 4x} \right) = -2 \cos 4x$ $3 \sin 4x + 2 \cos^2 4x = 0$ $3 \sin 4x + 2(1 - \sin^2 4x) = 0$ $-2 \sin^2 4x + 3 \sin 4x + 2 = 0$ $2 \sin^2 4x - 3 \sin 4x - 2 = 0$ $(2 \sin 4x + 1)(\sin 4x - 2) = 0$ $\sin 4x = -\frac{1}{2} \quad \text{or} \quad \sin 4x \neq 2$	<p>✓ identity</p> <p>✓ <math>1 - \sin^2 4x</math></p> <p>✓ standard form</p> <p>✓ factors</p> <p style="text-align: right;">(4)</p>
5.5.2	$\sin 4x = -\frac{1}{2}$ <p>ref. <math>\angle = 30^\circ</math></p> $4x = 210^\circ + k.360^\circ \quad \text{or} \quad 4x = 330^\circ + k.360^\circ$ $x = 52,5^\circ + k.90^\circ ; k \in Z \quad \quad \quad x = 82,5^\circ + k.90^\circ ; k \in Z$	<p>✓ <math>210^\circ ; 330^\circ</math></p> <p>✓ <math>52,5^\circ ; 82,5^\circ</math></p> <p>✓ <math>k.90^\circ ; k \in Z</math></p> <p style="text-align: right;">(3)</p>
		<b>[28]</b>

**QUESTION/VRAAG 6**

6.1	Period = $180^\circ$	✓ answer (1)
6.2		✓ x-intercepts ✓ turning points ✓ end points  (3)
6.3	$y \in [-1; 1]$ <b>OR/OF</b> $-1 \leq y \leq 1$	✓ answer (1)
6.4	$g(x) = -\cos 2x$ $g(x + 45^\circ) = -\cos 2(x + 45^\circ)$ $= -\cos(2x + 90^\circ)$ $= \sin 2x$	✓ $-\cos 2(x + 45^\circ)$  ✓ answer (2)
6.5.1	$x \in (-90^\circ; -45^\circ)$ <b>OR/OF</b> $-90^\circ < x < -45^\circ$	✓✓ $x \in (-90^\circ; -45^\circ)$ (2)
6.5.2	$2 \cos 2x - 1 > 0$ $\cos 2x > \frac{1}{2}$ $-\cos 2x < -\frac{1}{2}$ $x \in (-30^\circ; 30^\circ)$ <b>OR/OF</b> $-30^\circ < x < 30^\circ$	✓ $\cos 2x > \frac{1}{2}$ ✓ $-\cos 2x < -\frac{1}{2}$ ✓ $x = \pm 30^\circ$ ✓ interval (4)
		<b>[13]</b>

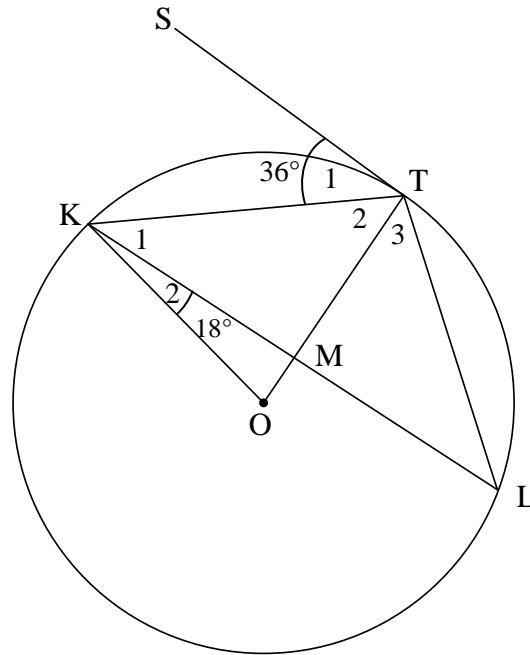
**QUESTION/VRAAG 7**



<p>7.1.1</p>	$\frac{AC}{20} = \cos 30^\circ$ $AC = 20 \cos 30^\circ$ $AC = 10\sqrt{3} = 17,32 \text{ units}$ <p><b>OR/OF</b></p> $\frac{AC}{\sin 60^\circ} = \frac{20}{\sin 90^\circ}$ $\therefore AC = 20 \sin 60 = 17,32$	<p>✓ trig ratio</p> <p>✓ answer (2)</p> <p>✓ trig ratio</p> <p>✓ answer (2)</p>
<p>7.1.2</p>	$AB^2 = AC^2 + BC^2 - 2AC \cdot BC \cos \hat{ACB}$ $AB^2 = (10\sqrt{3})^2 + 8^2 - 2(10\sqrt{3})(8) \cos 100^\circ$ $AB = 20,30 \text{ units}$	<p>✓ cosine formula</p> <p>✓ substitution into cosine formula</p> <p>✓ answer (3)</p>
<p>7.2</p>	$\frac{\sin \hat{ADB}}{AB} = \frac{\sin \hat{ABD}}{AD}$ $\frac{\sin \hat{ADB}}{20,3} = \frac{\sin 73,4^\circ}{20}$ $\sin \hat{ADB} = \frac{20,3 \sin 73,4^\circ}{20}$ $\hat{ADB} = 76,58^\circ$	<p>✓ sine formula in <math>\triangle ABD</math></p> <p>✓ substitution into sine formula</p> <p>✓ answer (3)</p>
<p><b>[8]</b></p>		

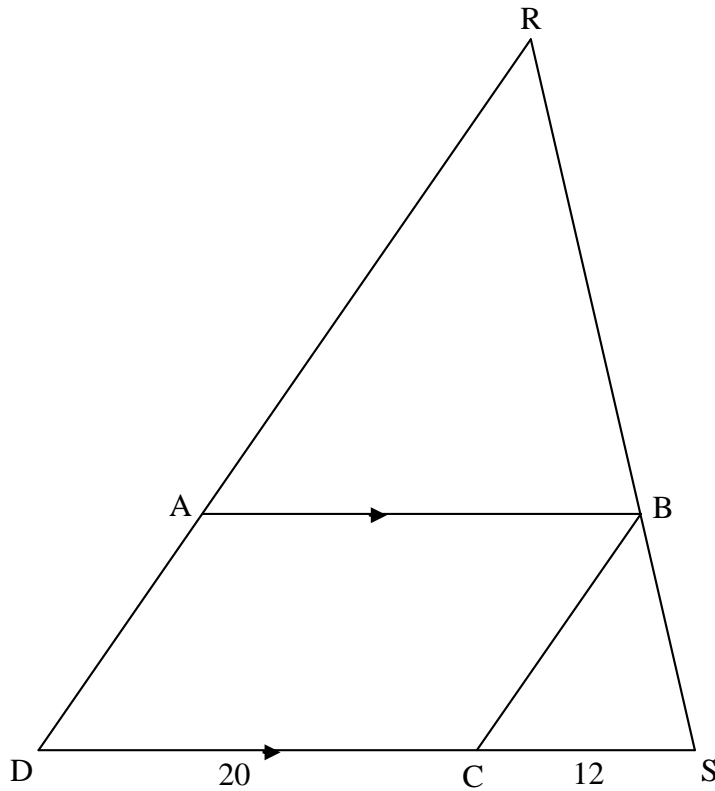
**QUESTION/VRAAG 8**

8.1



8.1.1(a)	$\hat{T}_2 = 54^\circ$ [tan $\perp$ rad]	✓ S ✓R (2)
8.1.1(b)	$\hat{L} = 36^\circ$ [tan - chord theorem]	✓ S ✓R (2)
8.1.1(c)	$\hat{KOT} = 72^\circ$ [ $\angle$ at centre = $2 \times \angle$ at circumference]  <b>OR/OF</b> $\hat{OKT} = \hat{T}_2 = 54^\circ$ [ $\angle$ s opposite = radii] $\hat{KOT} = 180^\circ - (54^\circ + 54^\circ)$ [sum of int $\angle$ 's of $\Delta$ ] $= 72^\circ$	✓ S ✓R (2)  ✓ S/R ✓ S (2)
8.1.2	$\hat{KMO} = 180^\circ - (18^\circ + 72^\circ)$ $= 90^\circ$ [sum of int $\angle$ 's of $\Delta$ ]  $\therefore KM = ML$ [line from centre $\perp$ to chord]  <b>OR/OF</b> $\hat{OKT} = 54^\circ$ [ $\angle$ s opposite = radii] $\hat{K}_1 = 54^\circ - 18^\circ = 36^\circ$ $\hat{TMK} = 90^\circ$ [sum of int $\angle$ 's of $\Delta$ ] $\therefore KM = ML$ [line from centre $\perp$ to chord]	✓ S ✓ S ✓ R (3)  ✓ S ✓ S ✓ R (3)

8.2



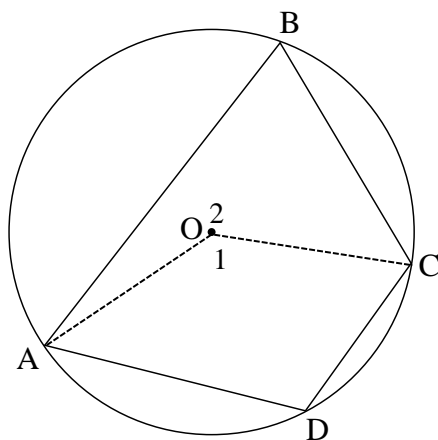
<p>8.2.1</p>	$\frac{DC}{CS} = \frac{20}{12} = \frac{5}{3}$ $\therefore \frac{DC}{CS} = \frac{RB}{BS}$ $\therefore BC \parallel DR \quad \text{[converse line } \parallel \text{ one side of } \Delta \text{ OR sides in the same proportion]}$ $\therefore BC \parallel AD$	<p>✓ S</p> <p>✓ S</p> <p>✓ R</p> <p>(3)</p>
<p>8.2.2</p>	$\frac{AR}{AD} = \frac{RB}{BS} \quad \text{[line } \parallel \text{ one side of } \Delta \text{] OR [ Prop Theorem AB } \parallel \text{ DS]}$ $\frac{AR}{AD} = \frac{5}{3}$ $\frac{48 - AD}{AD} = \frac{5}{3}$ $\therefore 5AD = 144 - 3AD$ $AD = 18$ $AB = 20 \quad \text{[opp sides of parm]}$ $\therefore AD : AB = 18 : 20 = 9 : 10$	<p>✓ <math>\frac{AR}{AD} = \frac{5}{3}</math></p> <p>✓ AD = 18</p> <p>✓ ratio</p> <p>(3)</p>



	<p><b>OR/OF</b></p> $\frac{AR}{RD} = \frac{5}{8} \dots\dots\dots \text{prop thm } AB \parallel DS$ $\frac{AR}{48} = \frac{5}{8}$ <p><math>\therefore AR = 30</math> and <math>AD = 18</math></p> $\therefore \frac{AR}{RD} = \frac{AB}{DS} \dots\dots\dots \parallel \Delta's$ <p><math>\therefore AB = 20</math></p> <p><math>\therefore AB : AD = 18 : 20 = 9 : 10</math></p>	<p>✓ <math>\frac{AR}{RD} = \frac{5}{8}</math></p> <p>✓ <math>AD = 18</math></p> <p>✓ ratio</p> <p>(3)</p>
		<p>[15]</p>

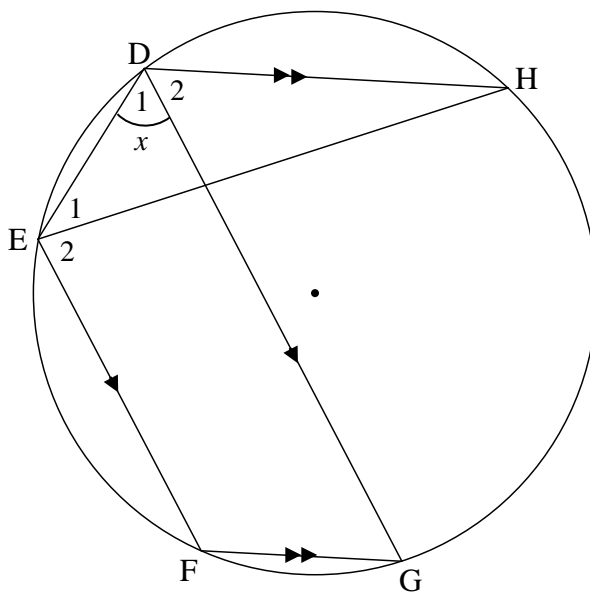
**QUESTION/VRAAG 9**

9.1



<p>9.1</p>	<p>Constr: Draw radii OA and OC.</p> <p>Proof:</p> <p><math>\hat{O}_1 = 2\hat{B}</math> [∠ at centre = 2×∠ at circumference]</p> <p><math>\hat{O}_2 = 2\hat{D}</math> [∠ at centre = 2×∠ at circumference]</p> <p><math>\hat{O}_1 + \hat{O}_2 = 360^\circ</math> [revolution]</p> <p><math>2\hat{B} + 2\hat{D} = 360^\circ</math> [revolution]</p> <p><math>\therefore \hat{B} + \hat{D} = 180^\circ</math></p>	<p>✓ Construction</p> <p>✓ S ✓ R</p> <p>✓ S/R</p> <p>✓ S</p> <p>(5)</p>
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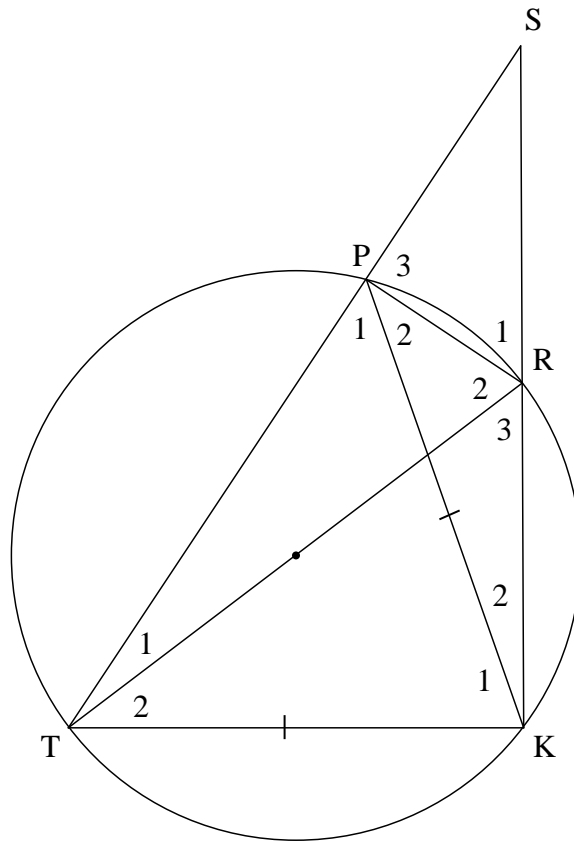
9.2



9.2	$\hat{EFG} = 180^\circ - \hat{D}_1$ $\therefore \hat{EFG} = 180^\circ - x$ $\hat{EFG} = 180^\circ - \hat{G}$ $\hat{G} = x$ But $\hat{G} = \hat{D}_2$ $\therefore \hat{D}_1 = \hat{D}_2 = x$	[opp $\angle$ 's of cyclic quad]  [co-int $\angle$ 's; $EF \parallel DG$ ]  [alt $\angle$ 's; $DH \parallel FG$ ]	$\checkmark S \checkmark R$  $\checkmark S / R$  $\checkmark S / R$  (4)
			<b>[9]</b>

**QUESTION/VRAAG 10**

10.1



10.1.1	$\hat{T}PR = 90^\circ$ $\hat{S}PR = 90^\circ$ $\therefore SR$ is a diameter  <b>OR</b>  $\hat{T}KR = 90^\circ$ $\hat{S}PR = 90^\circ$ $\therefore SR$ is a diameter  <b>OR</b>	[ $\angle$ in semi-circle ] [ $\angle$ 's on a straight line ] [ converse $\angle$ in semi-circle ]  [ $\angle$ in semi-circle ] [ ext $\angle$ of cyclic quad ] [ converse $\angle$ in semi-circle ] [ chord subtends a right angle ]	$\checkmark S \checkmark R$ $\checkmark S$ $\checkmark R$ (4)  $\checkmark S \checkmark R$ $\checkmark S$ $\checkmark R$ (4)
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<p>10.1.2</p>	<p><math>\hat{R}_1 = \hat{P}\hat{T}\hat{K}</math> [ext <math>\angle</math> of cyclic quad]  <math>\hat{P}_1 = \hat{P}\hat{T}\hat{K} = \hat{R}_1</math> [ <math>\angle</math>s opp equal sides]  <math>\hat{S} + \hat{R}_1 = \hat{P}_1 + \hat{P}_2</math> [ext <math>\angle</math> of <math>\Delta</math>]  <math>\therefore \hat{S} = \hat{P}_2</math> [<math>\hat{R}_1 = \hat{P}_1</math> ]</p>	<p>✓S ✓R                  ✓S /R                  ✓S ✓R                  (5)</p>
<p>10.1.3</p>	<p>In <math>\Delta</math>SPK and <math>\Delta</math>PRK  <math>\hat{S} = \hat{P}_2</math> [proved]  <math>\hat{K}_2 = \hat{K}_2</math> [common]  <math>\Delta</math>SPK <math>\parallel</math> <math>\Delta</math>PRK [<math>\angle, \angle, \angle</math> ]  <b>OR/OF</b>                  In <math>\Delta</math>SPK and <math>\Delta</math>PRK  <math>\hat{S} = \hat{P}_2</math> [proved]  <math>\hat{K}_2 = \hat{K}_2</math> [common]  <math>\hat{S}\hat{P}\hat{K} = \hat{P}\hat{R}\hat{K}</math> [sum of <math>\angle</math>s in <math>\Delta</math>]  <math>\Delta</math>SPK <math>\parallel</math> <math>\Delta</math>PRK</p>	<p>✓S                  ✓S                  ✓S/R                  (3)                  ✓S                  ✓S                  ✓S/R                  (3)</p>
<p>10.2</p>	<p><math>\frac{PK}{RK} = \frac{SK}{PK}</math> [<math>\Delta</math>SPK <math>\parallel</math> <math>\Delta</math>PRK]  <math>PK^2 = SK.RK</math>  <math>ST^2 = SK^2 + TK^2</math> [Pythagoras]  <math>TK = PK</math> [Given]  <math>ST^2 = SK^2 + PK^2</math>  <math>ST^2 = SK^2 + SK.RK</math>  <math>ST^2 = (2RK)^2 + 2RK.RK</math>  <math>ST^2 = 6RK^2</math>  <math>ST = \sqrt{6}RK</math></p>	<p>✓S                  ✓S                  ✓ <math>PK^2 = SK.RK</math>                  ✓ <math>SK = 2RK</math>                  ✓ <math>ST^2 = 6RK^2</math>                  (5)</p>
		<p>[17]</p>

**TOTAL/TOTAAL: 150**